

# Isekai Workshop

JUNE 2019





# A FRAMEWORK FOR ZERO-KNOWLEDGE COMPUTATIONS

- Isekai (<https://github.com/sikoba/isekai>)
- Prove the execution of arbitrary programs in Zero-Knowledge
- For any language
- Using any Zero-Knowledge Proof scheme
- Work in progress!



# ISEKAI ZERO-KNOWLEDGE PROOFS

- A *prover* can prove he executed a function  $f$  on some inputs

$$u = f(x,w) \quad u,x \text{ are public, } w \text{ are private}$$

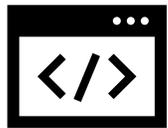
1. The *prover* sends the proof  $\pi$ , inputs  $x$ , output  $u$  and function  $f$  to a *verifier*



2. *Verifier* checks  $(\pi, u, x, f)$  is valid and is **convinced** that prover knows  $w$  such that  $u=f(x,w)$  with very high probability. *Verifiers* does **not** know  $w$ .
- Verification is **faster** than executing  $f(x,w)$

# ISEKAI HIGH-LEVEL WORKFLOW

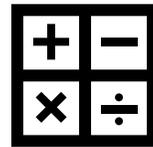
Computer program  
(source code)



Circuit



Equations  
system



Proof



# ISEKAI INPUT

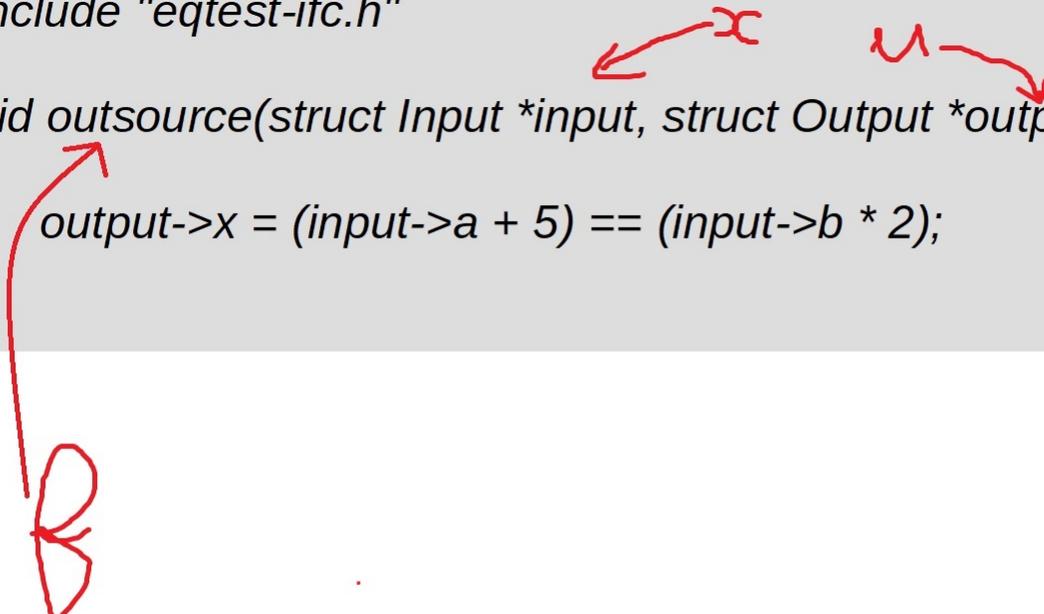
C source code, with a function 'outsource' having a specific signature

```
#include "eqtest-ifc.h"  
  
void outsource(struct Input *input, struct Output *output)  
{  
    output->x = (input->a + 5) == (input->b * 2);  
}
```

# ISEKAI INPUT

C source code, with a function outsource having a specific signature

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#include "eqtest-ifc.h"  
  
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{  
    output->x = (input->a + 5) == (input->b * 2);  
}
```



# ISEKAI INPUT

Zero-Knowledge Input



```
void outsource(struct Input *input, struct NzikInput * nzik, struct Output *output)
{
    output->x = (input->a + 5) == (nzik->b * 2);
}
```

# ISEKAI INPUT

MyFunction.c

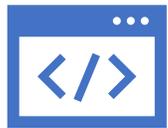
```
void outsource(struct Input *input, struct NzikInput * nzik, struct Output *output)
{
    output->x = (input->a + 5) == (nzik->b * 2);
}
```

MyFunction.c.in

```
3 // input (public)
1 // always 1
4 // nzik (private)
```

# ISEKAI HIGH-LEVEL WORKFLOW

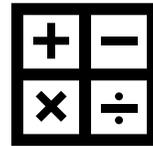
Computer program  
(source code)



Circuit



Equations  
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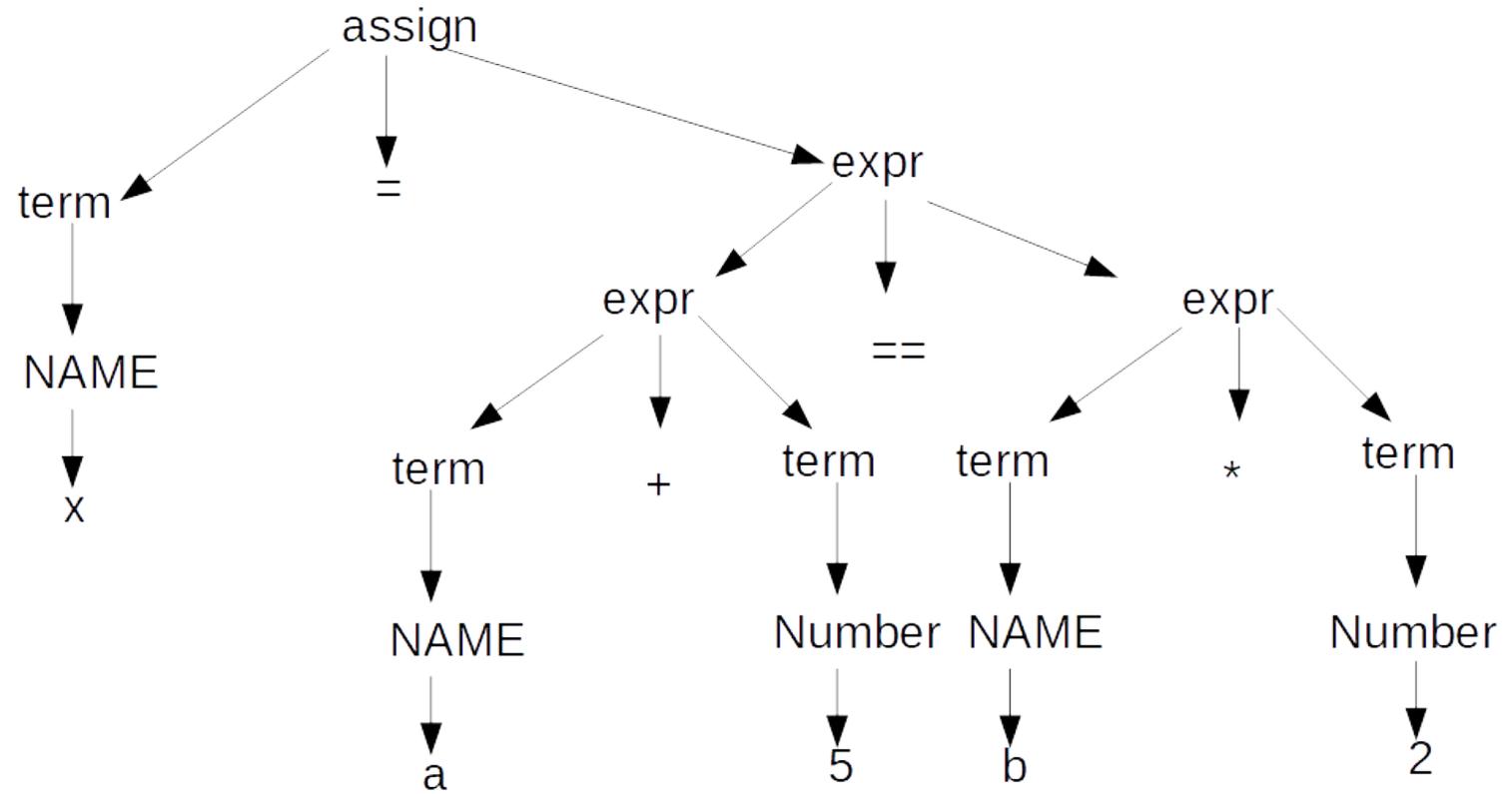


Proof



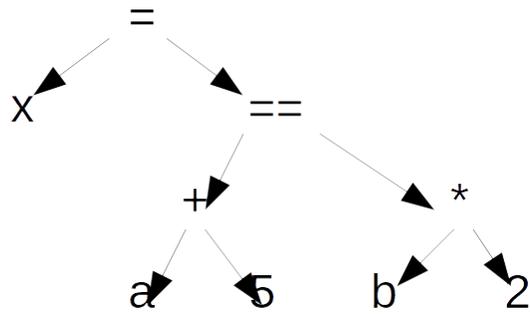
# PARSING

x = a+5 == b\*2



# ABSTRACT SYNTAX TREE

`x = a+5 == b*2`



AST

Parent Scope

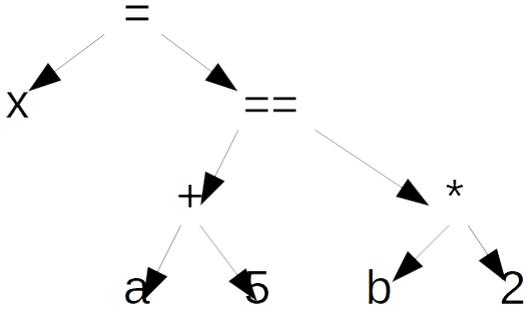
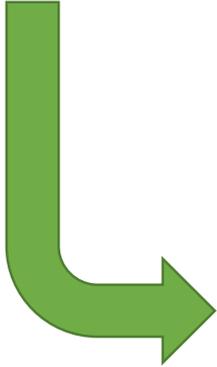


Key	Value
a	3
b	4
x	True

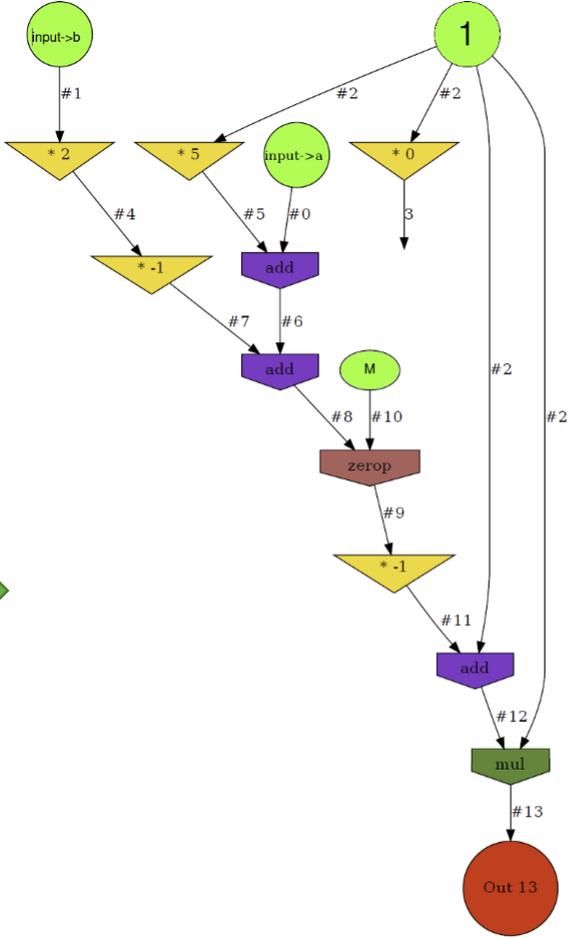
ADT (Symbol Table)

# ARITHMETIC CIRCUIT

$x = a + 5 == b * 2$



AST



Circuit

# GENERATE CIRCUIT WITH ISEKAI

```
Isekai/wk: ~$ ../isekai --arith=ex1.ari ex1.c
```

```
total 14
```

```
input 0 # input
```

```
input 1 # input
```

```
input 2 # one-input
```

```
const-mul-0 in 1 <2> out 1 <3> # zero
```

```
const-mul-2 in 1 <1> out 1 <4> # multiply-by-constant 2
```

```
const-mul-5 in 1 <2> out 1 <5> # constant 5
```

```
add in 2 <0 5> out 1 <6> # #<Isekai::ArithAddReq:0x7fff2e16db00>
```

```
const-mul-neg-1 in 1 <4> out 1 <7> # zerop subtract negative
```

```
add in 2 <6 7> out 1 <8> # zerop diff
```

```
zerop in 1 <8> out 2 <10 9> # zerop #<Isekai::ArithAddBus:0x7fff2e1ebdc0>
```

```
const-mul-neg-1 in 1 <9> out 1 <11> # zerop inverse
```

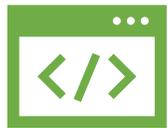
```
add in 2 <2 11> out 1 <12> # zerop result
```

```
mul in 2 <2 12> out 1 <13> # output-cast
```

```
output 13 #
```

# ISEKAI HIGH-LEVEL WORKFLOW

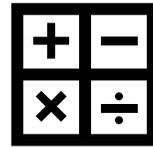
Computer program  
(source code)



Circuit



Equations  
system



Proof



# ISEKAI HIGH-LEVEL WORKFLOW

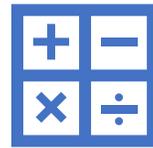
Computer program  
(source code)



Circuit



Equations  
system



Proof



# R1CS

Set of bilinear equations  $\langle A, B \rangle = C$

$$(a_0 + a_1 * x_1 + \dots + a_n * x_n) * (b_0 + b_1 * x_1 + \dots + b_n * x_n) = c_0 + c_1 * x_1 + \dots + c_n * x_n$$

$a_i, b_i, c_i$  are coefficients in a finite field

$x_i$  are the variables of the system

# RANK-1 CONSTRAINTS SYSTEM

```
#include "eqtest-ifc.h"
```

```
void outsource(struct Input *input, struct Output *output)  
{  
    output->x = (input->a + 5) == (input->b * 2);  
}
```

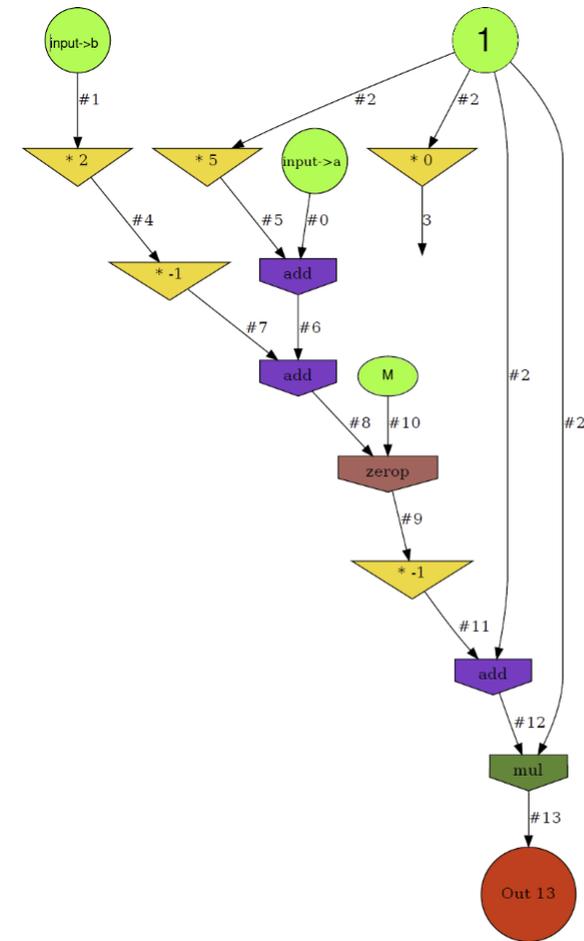
$$x_8 = x_0 + 5 - x_1 * 2$$

$$(1 - x_9) * x_8 = 0$$

$$x_8 * x_{10} - x_9 = 0$$

$$x_{13} = 1 - x_9$$

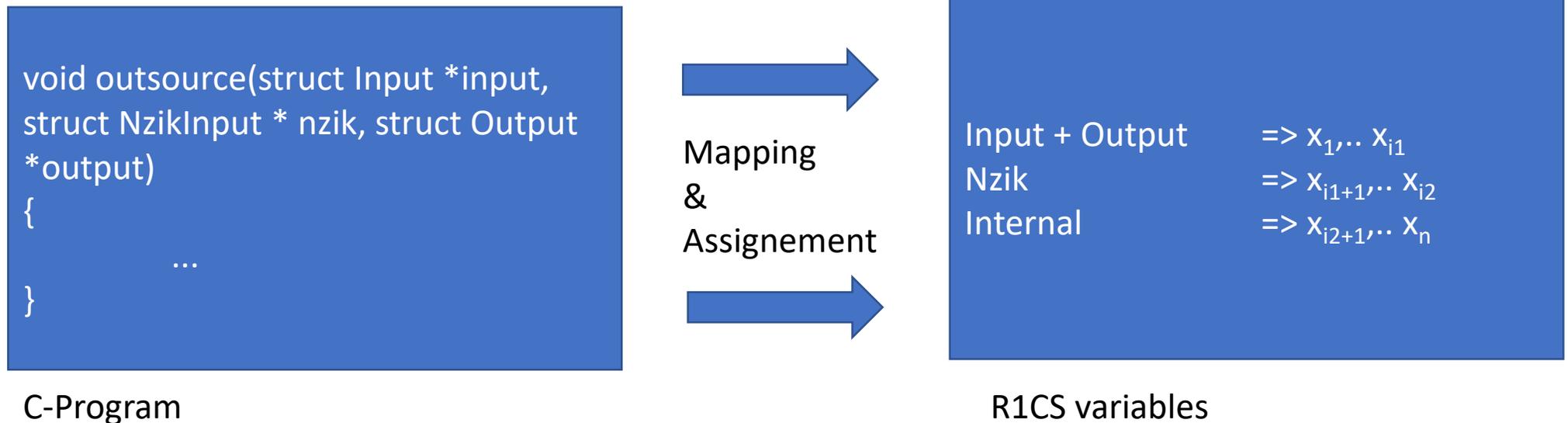
R1CS



Circuit

# R1CS REDUCTION

- R1CS variables represent the input data (both public and zero-knowledge) of the high-level statements as well internal variables
- The **mapping** of the variables is done during the R1CS reduction
- The values of the variables (assignment) is a solution to the R1CS and represent an execution of the program



# GENERATE R1CS WITH ISEKAI

```
Isekai/wk: ~$ ../isekai --r1cs=ex1.j1 ex1.c
```

```
(enter) Parsing and Evaluating the circuit [ ] (1561037885.1220s  
x0.00 from start)
```

```
(leave) Parsing and Evaluating the circuit [0.0023s x0.00]  
(1561037885.1243s x0.00 from start)
```

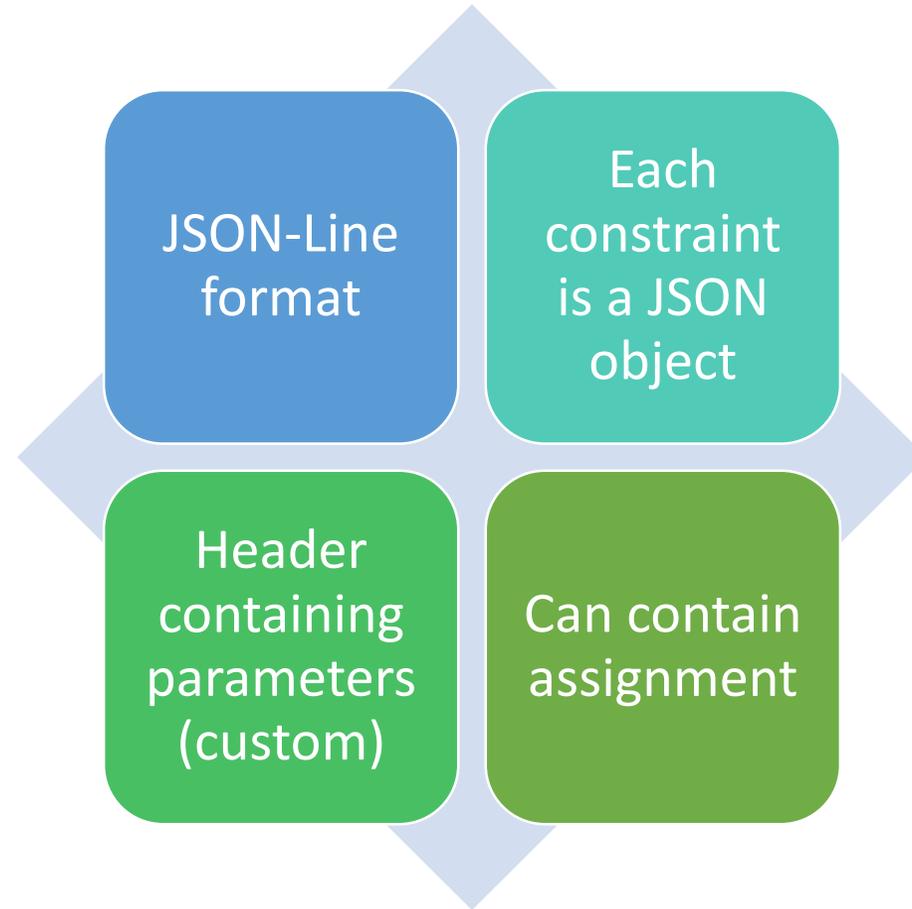
```
Translating Constraints ...
```

```
    Constraint translation done
```

```
    Memory usage for constraint translation: 0 MB
```

```
Assignment of values done ..
```

# J-R1CS



# PRO

**Extensibility**

**Implementation**

**Lightweight**

**Interoperability**

**Readability**

**Scalability**

# J-R1CS

```
{"r1cs":{"constraint_nb":3,"extension_degree":1,"field_characteristic":1,"instance_nb":4,"version":"1.0","witness_nb":3}}
```

```
{"A":[[0,"0"],[1,"1"],[2,"21888242871839275222246405745257275088548364400416034343698204186575808495615"],[3,"5"]],"B":[[0,"1"],[6,"21888242871839275222246405745257275088548364400416034343698204186575808495616"]],"C":[[0,"0"]]}
```

```
{"A":[[0,"0"],[1,"1"],[2,"21888242871839275222246405745257275088548364400416034343698204186575808495615"],[3,"5"]],"B":[[0,"0"],[7,"1"]],"C":[[0,"0"],[6,"1"]]}
```

```
{"A":[[0,"0"],[3,"1"]],"B":[[0,"0"],[3,"1"],[6,"21888242871839275222246405745257275088548364400416034343698204186575808495616"]],"C":[[0,"0"],[4,"1"]]}
```

# J-R1CS

```
{"r1cs":{"constraint_nb":3,"extension_degree":1,"field_characteristic":1,"instance_nb":4,"version":"1.0","witness_nb":3}}
```

```
{"A":[[0,"0"],[1,"1"],[2,"-2"],[3,"5"]],"B":[[0,"1"],[6,"-1"]],"C":[[0,"0"]]}
```

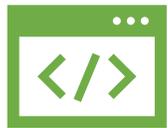
```
{"A":[[0,"0"],[1,"1"],[2,"-2"],[3,"5"]],"B":[[0,"0"],[7,"1"]],"C":[[0,"0"],[6,"1"]]}
```

```
{"A":[[0,"0"],[3,"1"]],"B":[[0,"0"],[3,"1"],[6,"-1"]],"C":[[0,"0"],[4,"1"]]}
```

```
{"inputs":["3","2","1","0"],"witnesses":["0","1","16416182153879456416684804308942956316411273300312025757773653139931856371713"]}
```

# ISEKAI HIGH-LEVEL WORKFLOW

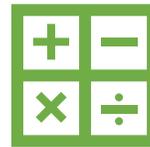
Computer program  
(source code)



Circuit



Equations  
system



Proof



# ZERO KNOWLEDGE PROOF



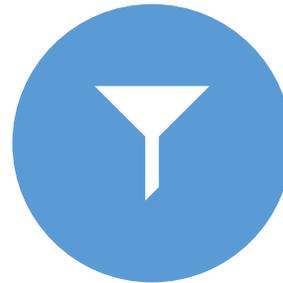
Source code is transformed into ***Equations*** system



Program execution is transformed into a ***Solution*** (assignment)



The system of equations provides the **constraint polynomial**



The Solution satisfies the constraints, they are the **roots** of the constraint polynomial

# GENERATING THE PROOF

1. Generate the trusted setup from the R1CS

$$\begin{matrix} \cdot \\ \cdot \\ (a_1x_1+\dots+a_nx_n)(b_1x_1+\dots+b_nx_n)=(c_1x_1+\dots+c_nx_n) \\ \cdot \\ \cdot \end{matrix}$$

R1CS



(EC generators, sampling points, randoms...)

Trusted Setup

2. Generate the proof from the trusted setup and the assignments

Trusted setup  
 $x_1, \dots, x_n$



$\pi$

3. Verify the proof

Trusted setup  
 $\pi$   
 $x_1, \dots, x_{i1}$



Success/Fail

# GENERATE PROOF

```
Isekai/wk: ~$ ../isekai --snark=ex1 ex1.j1
```

*\* The verification result2 is: PASS*

*Proved execution successfully with libSnark, generated:*

*Trusted setup : ex1.s*

*Proof: ex1.p*

# VERIFY PROOF

```
Isekai/wk: ~$ ../isekai --verif=ex1 ex1.j1.in
```

```
* The verification result2 is: PASS  
Congratulations, the proof is correct!
```

## EXAMPLE 2.

- $a, b \Rightarrow a + 5 < 2 * b$

```
#include "ex2.h"

void outsource(struct Input *input, struct Output *output)
{
    output->x = (input->a + 5) < (input->b * 2);
}
```

## EX3. ZERO-KNOWLEDGE

- $?,? \Rightarrow a+5-2*b$

```
#include "ex3.h"
```

```
void outsource(struct Input *input, struct NzikInput * nzik, struct Output *output)
{
    output->x = (nzik->a + 5) - (nzik->b * 2);
}
```

# MORE ADVANCED EXAMPLES

- Ex4. Median
- Ex5. Hash
- Ex6. Overflow



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